

Cubes and Squares

Student Activity

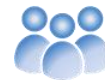
7 8 9 10 11 **12**



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Activity



Student

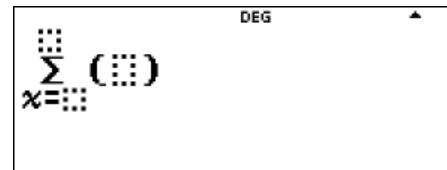
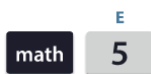


25 min

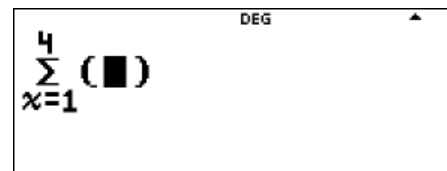
Calculator Instructions

The first part of this investigation involves summing cubed numbers: $1^3 + 2^3 + 3^3 + \dots + x^3 = \sum_{n=1}^x n^3$

The sum command can be found in the MATH menu.



To find the sum of the first 4 numbers cubed enter the numbers 1 and 4 accordingly:



The numbers need to be cubed **before** they are added.



Press **enter** to determine the result.

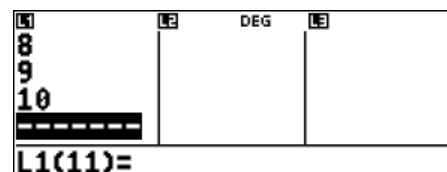
Question: 1.

Determine the sum of the first 10 numbers cubed: $1^3 + 2^3 + 3^3 + \dots + 10^3$.

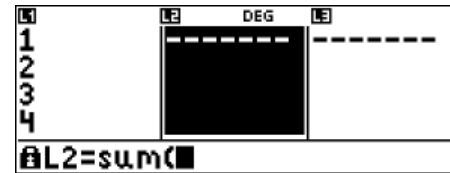
Question: 2.

Square the sum of the first 10 whole numbers and comment on the result: $(1 + 2 + 3 + \dots + 10)^2 = \left(\sum_{n=1}^x n \right)^2$

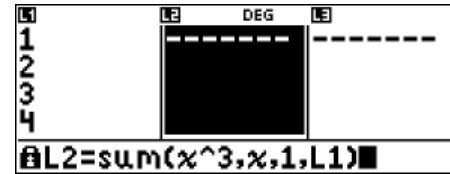
Enter the numbers 1 to 10 in List 1.




Navigate across to List 2 and enter the sum formula:

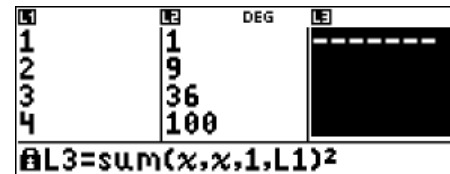


The syntax for the sum command in this environment is as follows: $\text{sum}(\text{expression}, \text{variable}, \text{start}, \text{end})$



Then press:  to execute the calculations.

List 3 needs to have a formula for the squared sum of whole numbers. The formula should be entered as shown opposite:



Question: 3.

Complete the following table of values:

N	1	2	3	4	5	6	7	8	9	10
N^3	1	8	27							
$\sum_{x=1}^n x^3$	1	9	36							
$\sum_{x=1}^n x$	1	3	6	10						
$\left(\sum_{x=1}^n x\right)^2$	1	9								

Question: 4.

Write down the formula for $\sum_{x=1}^n x$ and hence the formula for $\sum_{x=1}^n x^3$.

Question: 5.

Use induction to prove the formula for the sum of the first n^3 whole numbers.