# Vertical Asymptotes

Topic 1.9: Rational Functions and Vertical Asymptotes

**Vertical Asymptotes** 

## **Practice Problem 1**

The graph of function g has a vertical asymptote at x = -2. Which of the following expressions could define g(x)?

(2)	$(x+2)^4(x-5)^3$
(a)	$(x+2)^4(5-x)^2$

- (b)  $\frac{(x+2)^5(x-5)^2}{(x+2)^4(5-x)^3}$
- (c)  $\frac{(x+2)^4(x-5)^2}{(x+2)^5(5-x)^2}$
- (d)  $\frac{(x+2)^5(x-5)^3}{(x+2)^5(5-x)^3}$

### Practice Problem 2



The graphs of the polynomial functions g and h are shown. The function k(x) is defined by  $k(x) = \frac{g(x)}{h(x)}$ . What are the vertical asymptotes of the graph y = k(x)?

- (a) x = -1 and x = 2 only
- (b) x = -1 only
- (c) x = 2 only
- (d) x = 3 only



### Practice Problem 1 Solution:

(c) 
$$\frac{(x+2)^4(x-5)^2}{(x+2)^5(5-x)^2}$$

When the common factor of (x + 2) is reduced from the numerator and the denominator, there is a remaining (x + 2) in the denominator resulting in a vertical asymptote at x = -2.

### Practice Problem 2 Solution:

(a) x = -1 and x = 2 only

The function y = k(x) is undefined when h(x) = 0, this happens at x = -1 and x = 2. Since there are no common zeros in the numerator (where g(x) = 0), there are no holes, only vertical asymptotes.

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